## MEASURES OF DISPERSION

1. The Range
2. The Mean Deviation
3. he Semi-Interquartile Range
4. Percentile \& Decile
5. The Standard Deviation \& The Variance
6. Sheppard's Correction for Variance
7. Coefficient of Variation
> The Measures of central tendency gives us a birds eye view of the entire data they are called averages of the first order, it serve to locate the center of the distribution but they do not reveal how the items are spread out on either side of the central value. The measure of the scattering of items in a distribution about the average is called dispersion.
$>\quad$ Dispersion measures the extent to which the items vary from some central value. It may be noted that the measures of dispersion or variation measure only the degree but not the direction of the variation. The measures of dispersion are also called averages of the second order because they are based on the deviations of the different values from the mean or other measures of central tendency which are called averages of the first order.
$>$ In the words of Bowley "Dispersion is the measure of the variation of the items"
$>$ According to Conar "Dispersion is a measure of the extent to which the individual items vary"

## METHODS OF MEASURING DISPERSION

- Range
- Quartile Deviation
- Mean Deviation
- Standard Deviation

| Absolute measures of dispersion | Relative measures of dispersion |
| :--- | :--- |
| Range (R) | Coefficient of Range ( CR ) |
| Quartile Deviation (Q.D.) | Coefficient of Quartile Deviation (C.Q.D.) |
| Mean Deviation (M.D.) | Coefficient of Mean Deviation (C.M.D.) |
| Standard Deviation (S.D.) | Coefficient of Variation (C.V.) |

[^0]
## $>$ Range:

It is defined as the difference between the smallest and the largest observations in a given set of data.

| $\mathbf{R}=\mathrm{L}-\mathrm{S}$ |
| :--- |
| Where, L: largest Value, S: Smallest value |
| Coefficient of Range: $\mathrm{CR}=\frac{L-S}{L+S}$ |

## > Mean Deviation

It is also known as average deviation. In this case deviation taken from any average especially Mean, Median or Mode.
While taking deviation we have to ignore negative items and consider all of them as positive.

| Mean deviation from mean (M.D.) |
| :--- |
| $\overline{\boldsymbol{x}}=\frac{\sum_{i} f_{i} x_{i}}{\sum_{i} f_{i}}$ |
| M.D. $=\frac{\sum_{i} f_{i}\left\|x_{i}-\bar{x}\right\|}{\sum_{i} f_{i}}$ |
| Coefficient of Mean deviation |
| C.M.D. $=\frac{\text { M.D. }}{\bar{x}}$ |
| Mean deviation from A (M.D.) |
| M.D. $=\frac{\sum_{i} f_{i}\left\|x_{i}-A\right\|}{\sum_{i} f_{i}}$ |
| Where A is either mean , median or mode |

[^1]
## Quartile Deviation:

It is based on the quartiles so while calculating this may require upper quartile (Q3) and lower quartile (Q1) and then is divided by 2. Hence it is half of the deference between two quartiles it is also a semi inter quartile range.


## Deciles:

The values of the variate which divide the total frequency into ten equal parts are called deciles.
The formulas for computation are given by

$$
D_{1}=l+\frac{\frac{\bar{n}}{10}-c f}{f} \times i \quad, \quad D_{2}=l+\frac{\frac{2 n}{10}-c f}{f} \times i \quad \text { etc... }
$$

## Percentile:

The values of the variate which divide the total frequency into hundred equal parts, arte called percentiles. The formulas for computation are:

$$
P_{1}=l+\frac{\frac{n}{100}-c f}{f} \times i, P_{70}=l+\frac{\frac{70 n}{100}-c f}{f} \times i \text { etc } \ldots \ldots
$$

[^2]
## $>$ Standard Deviation:

The concept of standard deviation was first introduced by Karl Pearson in 1893.
The standard deviation is the most useful and the most popular measure of dispersion.
Just as the arithmetic mean is the most of all the averages, the standard deviation is the best of all measures of dispersion.

The standard deviation is represented by the Greek letter $\boldsymbol{\sigma}$ (sigma).
It is always calculated from the arithmetic mean.
S.D. $=\sigma=\sqrt{\frac{\sum f_{i} x_{i}{ }^{2}}{\sum f_{i}}-\bar{x}^{2}}$
$\bar{x}=\frac{\sum_{i} f_{i} x_{i}}{\sum_{i} f_{i}}$
Variance $=\sigma^{2}$
Coefficient of Variation
C.V. $=\frac{\text { S.D. }}{\bar{x}} * 100$

- Quartile deviation considers only $50 \%$ of the item and ignores the other $50 \%$ of items in the series.
- Mean deviation no doubt an improved measure but ignores negative signs without any basis.


## $>$ Combined Standard deviation

Let group of size $n_{1}$ having mean $\bar{x}_{1}$ and S.D. $\sigma_{1}$ is merged with another group of $n_{2}$, mean $\bar{x}_{2}$ and
S.D. $\sigma_{2}$, then S.D. of the combined group of size $n_{1}+n_{2}$ is given by

$$
\sigma=\sqrt{\frac{n_{1}\left(\sigma_{1}^{2}+d_{1}^{2}\right)+n_{2}\left(\sigma_{2}^{2}+d_{2}^{2}\right)}{n_{1}+n_{2}}}
$$

Where,

$$
d_{1}=\bar{x}_{1}-\bar{x} ; \quad \quad d_{2}=\bar{x}_{2}-\bar{x} ; \quad \bar{x}=\frac{n_{1} \cdot \bar{x}_{1}+n_{2} \cdot \bar{x}_{2}}{n_{1}+n_{2}}
$$

[^3]
## Sheppard's Correction for Variance:

In a grouped data the different observations are put into the same class.in the calculation of variation or standard deviation for grouped data, the frequency $f$ is multiplied by X which is the mid point of the respective classes.
Thus it is assumed that all the observations in the class are centered at X .
But this is not true, because the observations are spread in the said class.
This assumptions introduces some error in the calculation of standard deviation $(\boldsymbol{\sigma})$ or variance ( $\sigma^{2}$ )
The value can be corrected to some extent by applying Sheppard's correction,

$$
\begin{aligned}
& \sigma^{2}(\text { corrected })=\sigma^{2}-\frac{h^{2}}{12} \\
& \boldsymbol{\sigma}(\text { corrected })=\sqrt{\sigma^{2}-\frac{h^{2}}{12}}
\end{aligned}
$$

$h$ is uniform class interval

## - Corrected coefficient of variation:

## Corrected coefficient of variation $\sigma($ corrected $) * 100$

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